

Fundamentals of Imaging Colour Spaces

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Today's lesson

- All about colour spaces....
- All flavours, all species, all types

Alternative colour spaces

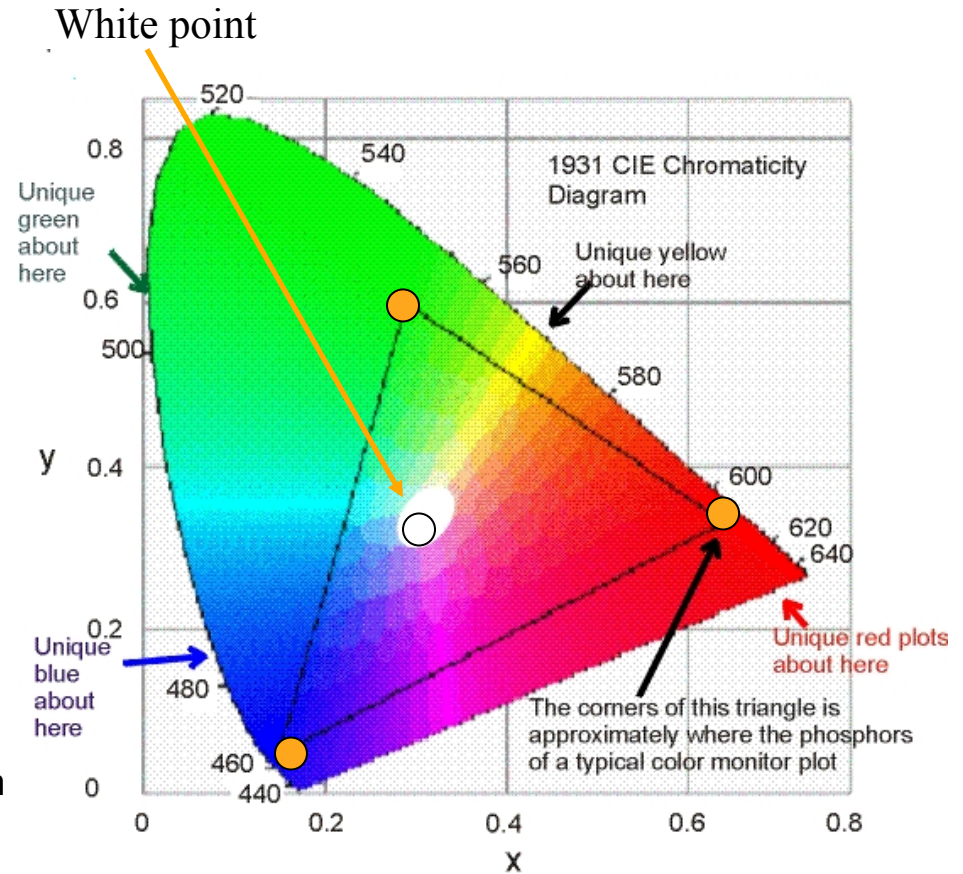
- In general, the XYZ colour space is not suitable for computing colours or encoding colours.
- Many XYZ pairs do not match viewable colours
- In most cases, alternative colour spaces are used
- Reasons for alternate colour spaces:
 - Physical constraints: I/O devices have different characteristics, and one might want to couple these to process colour directly
 - Efficient encoding: some colour spaces were developed for efficient encoding and transmission (NTSC, PAL)
 - Perceptual uniformity: make the colour space so that colour distances are perceptually sound
 - Intuitive usage: RGB is device oriented, and far from being easy to use

Transforming colour spaces

- Typically, the colour spaces are characterized by their bounding volumes in colour space
 - Called gamut of colours the space can represent
 - They usually do not cover all colours: for example, CRT screens can only add the phosphor colours.
- *Gamut mapping*: converting one gamut to another
 - For simple, linear, additive trichromatic displays the transformation from XYZ to their colour values can be usually given by a 3x3 matrix
 - This due to Grassman's law
 - Conversion is usually done with
 - a linear transformation to XYZ
 - some non-linear processing to minimize perceptual errors (e.g. gamma correction)

Transforming colour spaces

- To convert, one must know
 - Device primary colours
 - White point of the device
- These are usually described in x,y chromaticity coordinates.
- On the device, the primary colours are usually represented as points between 0 and 1 in 3D space (1,0,0), (0,1,0) (0,0,1).
- Why do I need the white point?
 - Simple: remember the CIE coordinates were projections.
 - So they do not contain luminance!
 - So we have no idea of their mutual strength
 - BUT if one knows the white point on the CIE, one knows the proportions of luminances (and know (1,1,1))
 - Table shows an example: ITU-R BT 709 colour space (HDTV)



	R	G	B	White
<i>x</i>	0.6400	0.3000	0.1500	0.3127
<i>y</i>	0.3300	0.6000	0.0600	0.3290

Transforming colour spaces

- Now, if one on top of this knows the luminance of the white point, one knows it all.
- If we know the xy coordinates of the points RGB we can compute $z=1-x-y$
- Thus, we can have the XYZ of RGB: (x_R, y_R, z_R) , (x_G, y_G, z_G) , (x_B, y_B, z_B) ,
- ...and of the white: (x_W, y_W, z_W) .
- Which gives following equations

$$X_W = x_R S_R + x_G S_G + x_B S_B,$$

$$Y_W = y_R S_R + y_G S_G + y_B S_B,$$

$$Z_W = z_R S_R + z_G S_G + z_B S_B.$$

where the S_x are scaling factors and unknown.

- This gives:
$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} x_R S_R & x_G S_G & x_B S_B \\ y_R S_R & y_G S_G & y_B S_B \\ z_R S_R & z_G S_G & z_B S_B \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

sRGB colour space

- On a typical display, such as CRT, plasma, LED and DLP, the phosphors are RGB.
- Since they may be different, the basic colors are in general different
- Therefore, there is no such thing as an RGB space: they are device dependent!
- You have therefore to convert to a standardized set of primaries.
- The space sRGB is exactly this standardization:
 - It assumes luminance as 80cd/m²
 - It uses a matrix computation

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9505 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

- ...and the following linearization transformation, which minimizes quantization errors in digital applications:

$$R_{\text{sRGB}} = \begin{cases} 1.055 R^{1/2.4} - 0.055 & R > 0.0031308, \\ 12.92 R & R \leq 0.0031308; \end{cases}$$

$$G_{\text{sRGB}} = \begin{cases} 1.055 G^{1/2.4} - 0.055 & G > 0.0031308, \\ 12.92 G & G \leq 0.0031308; \end{cases}$$

$$B_{\text{sRGB}} = \begin{cases} 1.055 B^{1/2.4} - 0.055 & B > 0.0031308, \\ 12.92 B & B \leq 0.0031308. \end{cases}$$

this is called *gamma encoding*

- This is NOT gamma correction!
It can be parametrized as:

$$R_{\text{nonlinear}} = \begin{cases} (1+f)R^\gamma - f & t < R \leq 1, \\ sR & 0 \leq R \leq t; \end{cases}$$

$$G_{\text{nonlinear}} = \begin{cases} (1+f)G^\gamma - f & t < G \leq 1, \\ sG & 0 \leq G \leq t; \end{cases}$$

$$B_{\text{nonlinear}} = \begin{cases} (1+f)B^\gamma - f & t < B \leq 1, \\ sB & 0 \leq B \leq t. \end{cases}$$

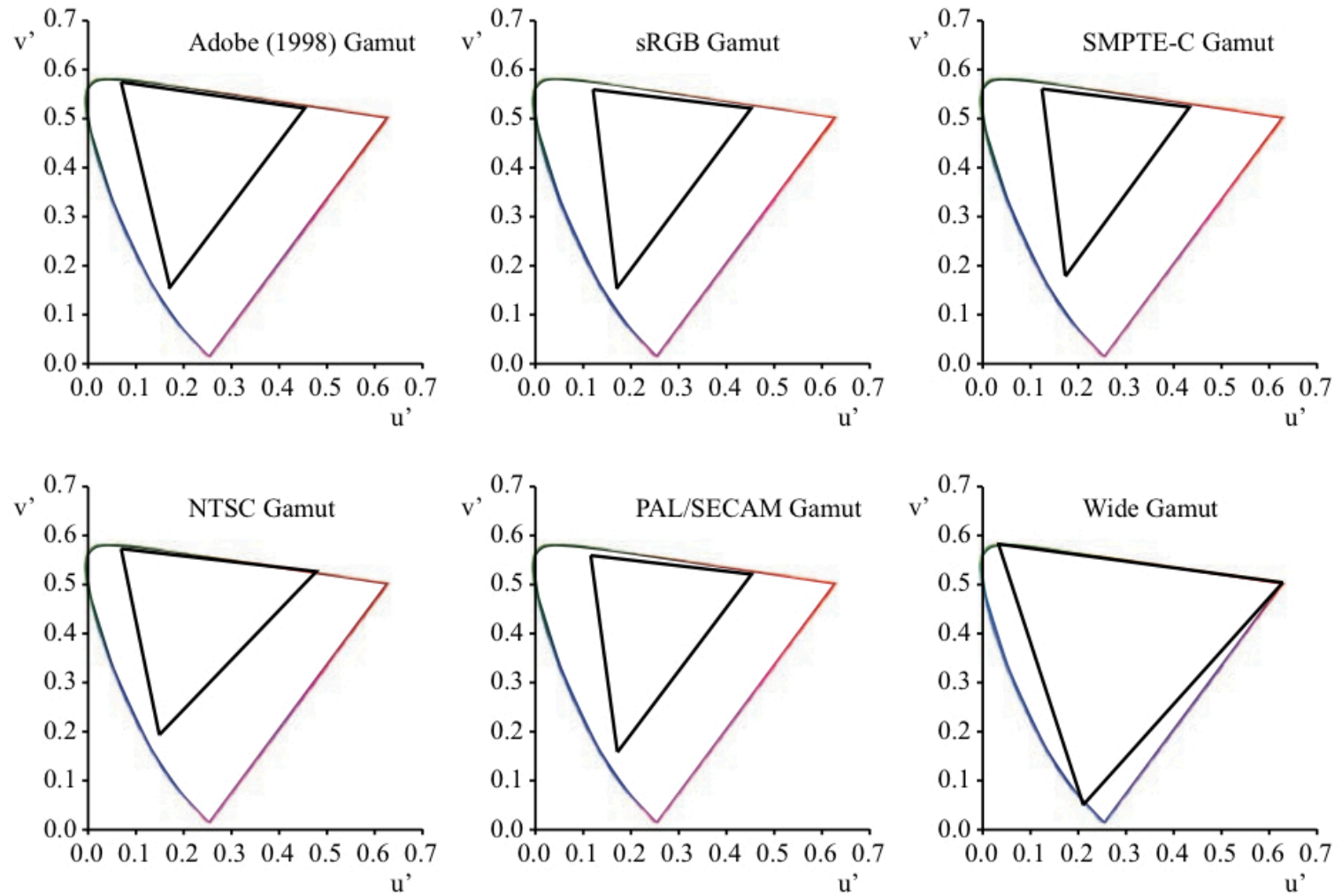
RGB Colour spaces

- In the course of time many standards have been developed, depending on their application:
 - Print
 - Screen
 - Draw
 - Net

Color space	XYZ to RGB matrix	RGB to XYZ matrix	Non-linear transform
sRGB	$\begin{bmatrix} 3.2405 & -1.5371 & -0.4985 \\ -0.9693 & 1.8760 & 0.0416 \\ 0.0556 & -0.2040 & 1.0572 \end{bmatrix}$	$\begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9505 \end{bmatrix}$	$\gamma = 1/2.4 \approx 0.42$ $f = 0.055$ $s = 12.92$ $t = 0.0031308$
Adobe RGB (1998)	$\begin{bmatrix} 2.0414 & -0.5649 & -0.3447 \\ -0.9693 & 1.8760 & 0.0416 \\ 0.0134 & -0.1184 & 1.0154 \end{bmatrix}$	$\begin{bmatrix} 0.5767 & 0.1856 & 0.1882 \\ 0.2974 & 0.6273 & 0.0753 \\ 0.0270 & 0.0707 & 0.9911 \end{bmatrix}$	$\gamma = \frac{1}{2.35} \approx \frac{1}{2.2}$ $f = \text{N.A.}$ $s = \text{N.A.}$ $t = \text{N.A.}$
HDTV (HD-CIF)	$\begin{bmatrix} 3.2405 & -1.5371 & -0.4985 \\ -0.9693 & 1.8760 & 0.0416 \\ 0.0556 & -0.2040 & 1.0572 \end{bmatrix}$	$\begin{bmatrix} 0.4124 & 0.3576 & 0.1805 \\ 0.2126 & 0.7152 & 0.0722 \\ 0.0193 & 0.1192 & 0.9505 \end{bmatrix}$	$\gamma = 0.45$ $f = 0.099$ $s = 4.5$ $t = 0.018$
NTSC (1953)/ ITU-R BT.601-4	$\begin{bmatrix} 1.9100 & -0.5325 & -0.2882 \\ -0.9847 & 1.9992 & -0.0283 \\ 0.0583 & -0.1184 & 0.8976 \end{bmatrix}$	$\begin{bmatrix} 0.6069 & 0.1735 & 0.2003 \\ 0.2989 & 0.5866 & 0.1145 \\ 0.0000 & 0.0661 & 1.1162 \end{bmatrix}$	$\gamma = 0.45$ $f = 0.099$ $s = 4.5$ $t = 0.018$
PAL/SECAM	$\begin{bmatrix} 3.0629 & -1.3932 & -0.4758 \\ -0.9693 & 1.8760 & 0.0416 \\ 0.0679 & -0.2289 & 1.0694 \end{bmatrix}$	$\begin{bmatrix} 0.4306 & 0.3415 & 0.1783 \\ 0.2220 & 0.7066 & 0.0713 \\ 0.0202 & 0.1296 & 0.9391 \end{bmatrix}$	$\gamma = 0.45$ $f = 0.099$ $s = 4.5$ $t = 0.018$
SMPTE-C	$\begin{bmatrix} 3.5054 & -1.7395 & -0.5440 \\ -1.0691 & 1.9778 & 0.0352 \\ 0.0563 & -0.1970 & 1.0502 \end{bmatrix}$	$\begin{bmatrix} 0.3936 & 0.3652 & 0.1916 \\ 0.2124 & 0.7010 & 0.0865 \\ 0.0187 & 0.1119 & 0.9582 \end{bmatrix}$	$\gamma = 0.45$ $f = 0.099$ $s = 4.5$ $t = 0.018$
Wide Gamut	$\begin{bmatrix} 1.4625 & -0.1845 & -0.2734 \\ -0.5228 & 1.4479 & 0.0681 \\ 0.0346 & -0.0958 & 1.2875 \end{bmatrix}$	$\begin{bmatrix} 0.7164 & 0.1010 & 0.1468 \\ 0.2587 & 0.7247 & 0.0166 \\ 0.0000 & 0.0512 & 0.7740 \end{bmatrix}$	$\gamma = \text{N.A.}$ $f = \text{N.A.}$ $s = \text{N.A.}$ $t = \text{N.A.}$

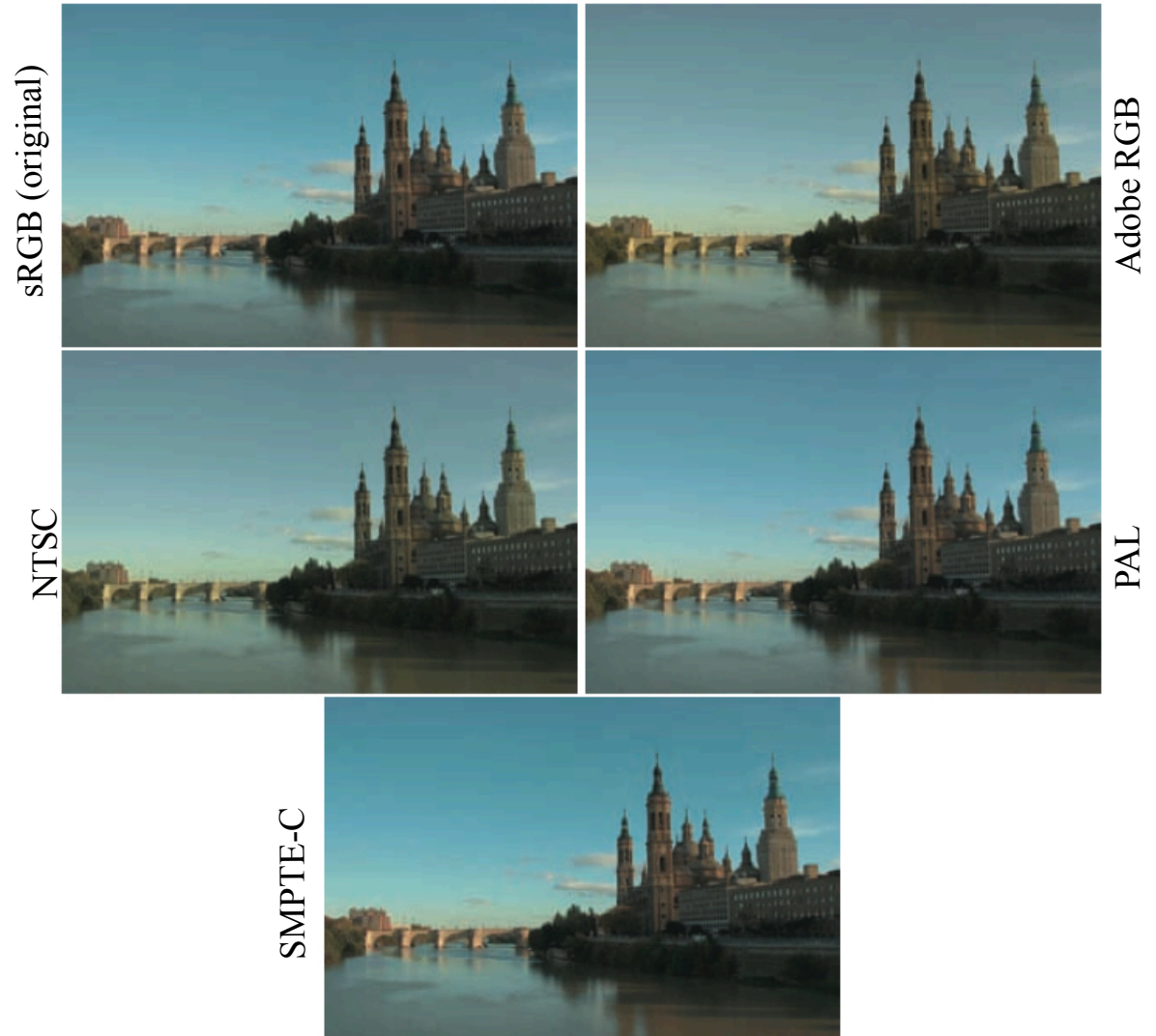
RGB Colour spaces

- Here the corresponding colour space gamuts:



RGB Colour spaces

- Converting modifies colours:

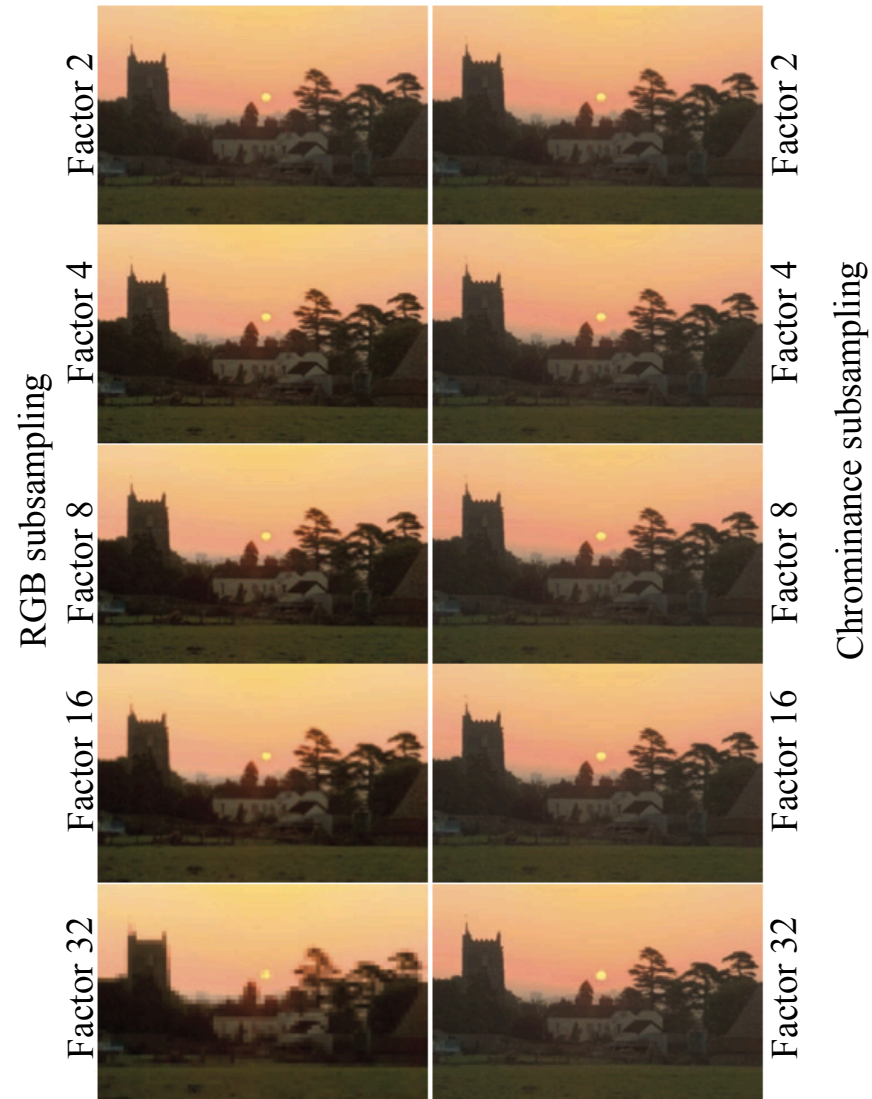


CMY and CMYK

- CMY and CMYK are used for printers:
 - Cyan
 - Magenta
 - Yellow
 - These are *subtractive* colours: printers deposit pigments subtracting light.
 - Inherently device dependent: ink has pigments
 - Usually, K (=black) is added, because $C+Y+M$ is never real black
 - Modern printers use many more primary colours, but we focus on 4 colour ones
- Here,
$$C=1-R$$
$$M=1-G$$
$$Y=1-B.$$
 - If one has K, then
$$K=Min(C,M,Y)$$
$$C=1-R$$
$$M=1-G$$
$$Y=1-B.$$

Luminance-Chrominance

- RGB is useful especially for hardware devices and transmission efficiency
- For intuition, it is easier to work with
 - one luminance channel
 - Two chrominance channels
- Luminance represents how light or dark (similar to Y channel)
 - Note that this can be used at the same time for B/W transmission
- Chrominance determine chromatic content
- Similar to visual system:
 - Rods sense luminance
 - Cones sample colour, in two colour-opposing axes:
 - Reddish-greenish
 - Blueish-yellowish
 - Because of this, colour spatial resolution (pixel) is only on the area of 4 cones
 - It is therefore possible to transmit colour at a lower resolution without a major quality decrease



CIE Yxy and YUV

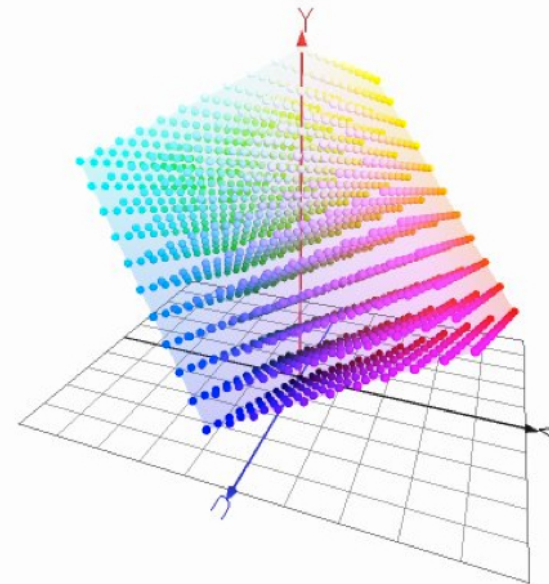
- The CIE Yxy can be seen as a colour space itself
 - Y carries luminance
 - Although xy do not match the eye sensors (color wise), nor do they map perceptual distances well
- As an alternative, the Cie proposed the space YUV:
 - Keep the Y of XYZ and Yxy
 - Map the other two coordinates so they are uniform:

$$u = \frac{2x}{6y - x + 1.5},$$
$$v = \frac{3y}{6y - x + 1.5}.$$

- CIE corrected later to improve uniformity into the CIE Yu'v' space:

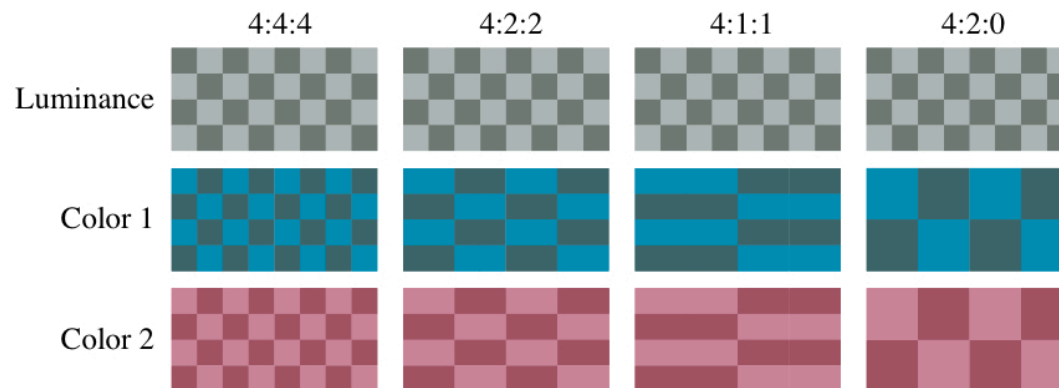
$$u' = \frac{2x}{6y - x + 1.5},$$
$$v' = \frac{4.5y}{6y - x + 1.5}.$$

nice about these spaces: since they are defined from Yxy, they are device independent



Broadcasting

- For broadcasting, luminance-chrominance systems are well suited
- Chrominance can be subsampled, as seen a few slides ago
- Typical subsamplings are done for both chroma components:
 - Here, a:b:c means:
 - a: luminance sampling WRT a sampling rate of 3.375 MHz
 - b: chrominance horizontal factor with respect to a
 - c: either the same as b, or 0 when the vertical resolution is subsampled at a factor of 2
caveat! CONSTANT 2!
 - So 4:2:2 means
 - luminance sampled at 13.5 MHz,
 - horizontal chrominance subsampled at factor 2,
 - vertical not subsampled



Broadcast colour spaces: PAL and NTSC

- We saw that broadcasting converts the RGB signal into a composite one for analog broadcasting
- In PAL, we saw before how R'G'B' is obtained from XYZ.
- From this, the luminance Y' is subtracted from R' and B' to obtain the chroma components

$$U' = 0.492111(B' - Y'),$$

$$V' = 0.877283(R' - Y').$$

this leads to the following transforms for the transmission variables Y'U'V':

$$\begin{bmatrix} Y' \\ U' \\ V' \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ -0.147141 & -0.288869 & 0.436010 \\ 0.614975 & -0.514965 & -0.100010 \end{bmatrix} \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix}$$

- NTSC uses instead the Y'I'Q' coordinates, defined as

$$I' = -0.27(B' - Y') + 0.74(R' - Y'),$$

$$Q' = 0.41(B' - Y') + 0.48(R' - Y').$$

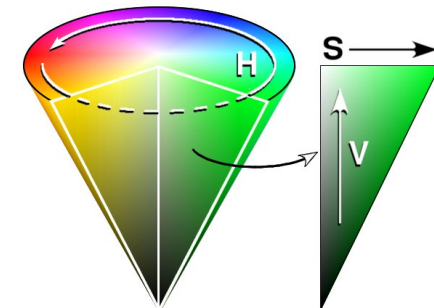
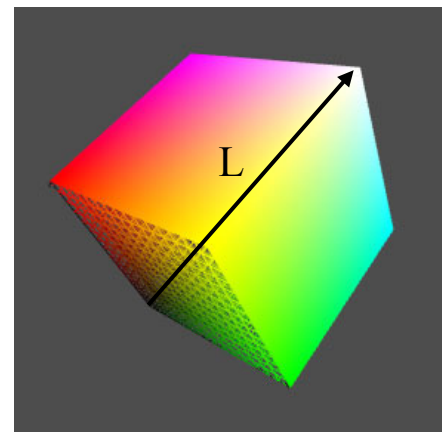
- I' is orange-blue
- Q': purple-green
- They lead to the transformation

$$\begin{bmatrix} Y' \\ I' \\ Q' \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.275 & -0.321 \\ 0.212 & -0.523 & 0.311 \end{bmatrix} \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix}$$

- Quite recently, these standards have been replaced by SMPTE-C and the HDTV standards
 - similar transformation matrices
 - not yet stable (see HD+)

HSL space

- Until now we introduced colour spaces defined for the hardware or transmission.
- Their main flaw is usability, since it is difficult to understand how their variables work
- A space that overcomes this is the Hue, Saturation and Lightness space (HSL)
- HSL comes in a few variants:
 - HIS (intensity)
 - HSV (value)
- These spaces are defined on the basis of an abstract RGB space which is supposed to be normalized
- Rotate RGB so that the diagonal forms the lightness axis
- Perpendicular to the lightness axis is a circular plane which defines color
 - Saturation: distance of the point on the circular plane to the lightness axis
 - Hue: angle between predetermined reference colour and colour we are interested in.



HSI and HSV spaces

- For HSI: by using the intermediate variables

$$v_{\min} = \min(R, G, B)$$

$$h = \frac{1}{360} \cos^{-1} \left(\frac{\frac{R-G}{2} + (R-B)}{\sqrt{(R-G)^2 + (R-B)(G-B)}} \right)$$

we obtain

$$I = \frac{R+G+B}{3},$$

$$S = 1 - \frac{v_{\min}}{I},$$

$$H = \begin{cases} 1-h & \text{if } \frac{B}{I} > \frac{G}{I} \wedge S > 0, \\ h & \text{if } \frac{B}{I} \leq \frac{G}{I} \wedge S > 0, \\ \text{undefined} & \text{if } S = 0. \end{cases}$$

- For HSV, the minimum and maximum of the RGB triplets are computed:

$$v_{\min} = \min(R, G, B),$$

$$v_{\max} = \max(R, G, B).$$

Then HSV are derived:

$$S = \frac{v_{\max} - v_{\min}}{v_{\max}},$$

$$V = v_{\max}.$$

$$H = \begin{cases} 60 \frac{G-B}{v_{\max} - v_{\min}} & \text{if } R = v_{\max}, \\ 60 \left(2 + \frac{B-R}{v_{\max} - v_{\min}} \right) & \text{if } G = v_{\max}, \\ 60 \left(4 + \frac{R-G}{v_{\max} - v_{\min}} \right) & \text{if } B = v_{\max}. \end{cases}$$

- Notice that H is in angle degrees, and that when R=G=B we have a gray value, and H is undefined.

LMS cone excitation space

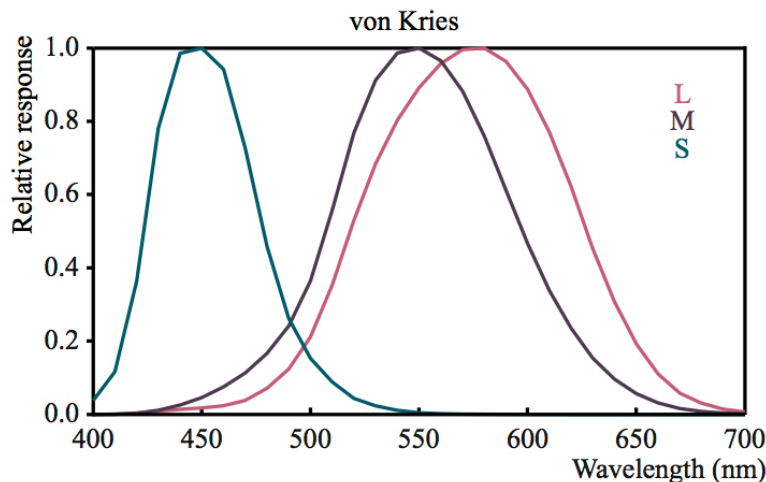
- Although the CIE XYZ functions are closely related to a linear transform of the LMS cone signals, they are not exact, and an approximation is needed
- A widely used approximation is the Hunt-Pointer-Estevéz cone fundamentals, which are used in colour appearance models

- Remember:
 - L=long wavelength,
 - M=middle wavelength
 - S=short wavelength
- Conversion from XYZ to LMS is simply given through the transforms:

$$\begin{bmatrix} L \\ M \\ S \end{bmatrix} = \begin{bmatrix} 0.3897 & 0.6890 & -0.0787 \\ -0.2298 & 1.1834 & 0.0464 \\ 0.0000 & 0.0000 & 1.0000 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

the inverse of which is

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 1.9102 & -1.1121 & 0.2019 \\ 0.3710 & 0.6291 & 0.0000 \\ 0.0000 & 0.0000 & 1.0000 \end{bmatrix} \begin{bmatrix} L \\ M \\ S \end{bmatrix}$$



Colour opponent spaces

- Characterized through
 - One achromatic variable
 - Two channels representing colour opponency
 - Usually red-green opponency+blue-yellow opponency
- We will examine two of these spaces:
 - CIE L*a*b* (CIELAB)
 - CIE L*u*v* (CIELUV)
 - Both standardized in 1976
- These spaces are interesting because they use a non-linear compression to achieve perceptual uniformity
- This perceptual uniformity is useful because it allows to compute colour differences by simply computing Euclidean distance in the space
- Finally, we will introduce the $L\alpha\beta$ space
- This last space was designed by applying principal component analysis to a set of pictures, encoded first in the LMS space

CIE 1976 L*a*b*

- Input to CIE L*a*b* are
 - (X,Y,Z), the stimulus tristimulus values
 - Tristimulus values of a diffuse white reflecting surface lit by a known illuminant (X_n, Y_n, Z_n)
- Equations calculate
 - the lightness L* of a colour
 - Two opponent chromatic channels, a* and b*

$$\begin{bmatrix} L^* \\ a^* \\ b^* \end{bmatrix} = \begin{bmatrix} 0 & 116 & 0 & -16 \\ 500 & -500 & 0 & 0 \\ 0 & 200 & -200 & 0 \end{bmatrix} \begin{bmatrix} f(X/X_n) \\ f(Y/Y_n) \\ f(Z/Z_n) \\ 1 \end{bmatrix}$$

where the function f is defined as

$$f(r) = \begin{cases} \sqrt[3]{r} & \text{for } r > 0.008856, \\ 7.787r + \frac{16}{116} & \text{for } r \leq 0.008856. \end{cases}$$

- The inverse is

$$X = X_n \begin{cases} \left(\frac{L^*}{116} + \frac{a^*}{500} + \frac{16}{116} \right)^3 & \text{if } L^* > 7.9996, \\ \frac{1}{7.787} \left(\frac{L^*}{116} + \frac{a^*}{500} \right) & \text{if } L^* \leq 7.9996, \end{cases}$$

$$Y = Y_n \begin{cases} \left(\frac{L^*}{116} + \frac{16}{116} \right)^3 & \text{if } L^* > 7.9996, \\ \frac{1}{7.787} \frac{L^*}{116} & \text{if } L^* \leq 7.9996, \end{cases}$$

$$Z = Z_n \begin{cases} \left(\frac{L^*}{116} - \frac{b^*}{200} + \frac{16}{116} \right)^3 & \text{if } L^* > 7.9996, \\ \frac{1}{7.787} \left(\frac{L^*}{116} - \frac{b^*}{200} \right) & \text{if } L^* \leq 7.9996. \end{cases}$$

- What is interesting of CIELAB is that it is almost perceptually linear, so one can compute Euclidean distances between colours:

E=Empfindung

$$\Delta E_{ab}^* = \left[(\Delta L^*)^2 + (\Delta a^*)^2 + (\Delta b^*)^2 \right]^{1/2}$$

CIE 1976 L*u*v*

- Input to CIE L*u*v* are like CIELAB:
 - (X,Y,Z), the stimulus tristimulus values
 - Tristimulus values of a diffuse white reflecting surface lit by a known illuminant (X_n, Y_n, Z_n)

- Here

$$L^* = \begin{cases} 116 \left(\frac{Y}{Y_n} \right)^{1/3} - 16 & \frac{Y}{Y_n} > 0.008856 \\ 903.3 \frac{Y}{Y_n} & \frac{Y}{Y_n} \leq 0.008856 \end{cases}$$

$$u^* = 13L^*(u' - u'_n),$$

$$v^* = 13L^*(v' - v'_n).$$

where

$$u' = \frac{4X}{X + 15Y + 3Z},$$

$$v' = \frac{9Y}{X + 15Y + 3Z},$$

$$u'_n = \frac{4X_n}{X_n + 15Y_n + 3Z_n},$$

$$v'_n = \frac{9Y_n}{X_n + 15Y_n + 3Z_n}$$

- Also CIELUV is perceptually more or less linear, which means that one can calculate distances

$$\Delta E_{uv}^* = \left[(\Delta L^*)^2 + (\Delta u^*)^2 + (\Delta v^*)^2 \right]^{1/2}$$

where the Δ represent differences in the respective components

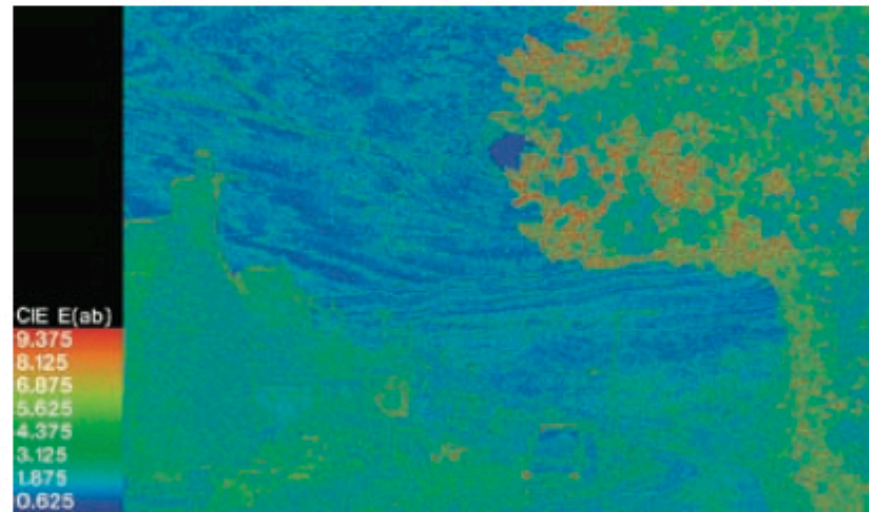
Colour metrics example: E^*_{ab}



Lossless: PPM



Compressed: JPG



Difference E^*_{ab} : CIELAB works well on small differences

L α β space

- For L α β , a set of natural images was used
- Then converted into LMS space
- And finally principal component analysis was done: rotating the data so that the first component captures most of the variance
- Then axes are rotated to coincide with first principal component
- Same is done for
 - 2nd principal component
 - 3rd principal component
- What results is a 3x3 transformation matrix
- In the first axis, one has luminance
- Second and third axes are yellow-blue and red-green components

$$\begin{bmatrix} L \\ \alpha \\ \beta \end{bmatrix} = \begin{bmatrix} \frac{1}{\sqrt{3}} & 0 & 0 \\ 0 & \frac{1}{\sqrt{6}} & 0 \\ 0 & 0 & \frac{1}{\sqrt{2}} \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & -2 \\ 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} \log L \\ \log M \\ \log S \end{bmatrix}$$



L*C*h_{ab} space

- This space can be seen as CIELAB expressed in polar coordinates instead of rectangular
- Conversion from CIELAB is done as follows:

$$L_{ab}^* = L^*,$$

$$C_{ab}^* = \sqrt{a^{*2} + b^{*2}},$$

$$h_{ab} = \tan^{-1} \left(\frac{b^*}{a^*} \right)$$

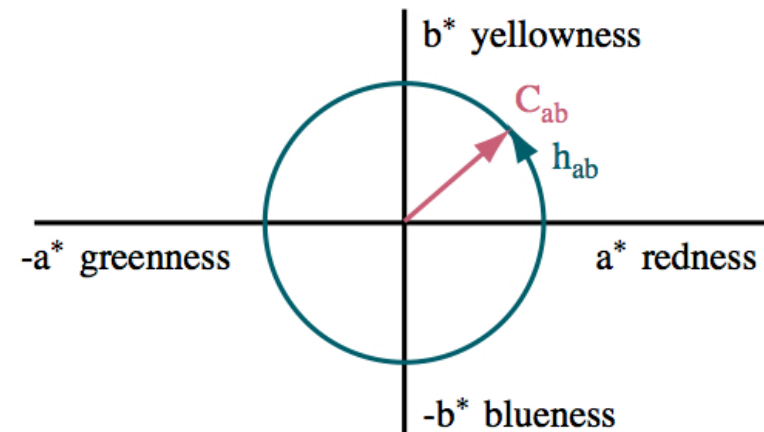
- C* defines chroma
- H_{ab} defines a hue (angle)
- Space is easier to understand for users
- If Lightness fixed, then colour can be expressed
 - along red-green and yellow-blue axes, or
 - As hue-chroma pair

- Colour difference can be specified by calculating rectangular hue difference:

$$\Delta H_{ab}^* = \left[(\Delta E^*)^2 - (\Delta L_{ab}^*)^2 - (\Delta C_{ab}^*)^2 \right]^{1/2}$$

$$\Delta E_{ab}^* = \left[(\Delta L^*)^2 + (\Delta C_{ab}^*)^2 + (\Delta H_{ab}^*)^2 \right]^{1/2}$$

- Inverse to CIELAB: $L^* = L^*$,
 $a^* = C^* \cos(h_{ab})$
 $b^* = C^* \sin(h_{ab})$.



Colour Difference Metrics: CMC (l:c)

- CIELAB and CIELUV are not as perceptually uniform as needed
- In 1984 the Colour Measurement Committee of the Society of Dyers and Colourists developed the CMC colour difference metric.
- Elaboration of CIELAB color difference, derived from LCH color space
- It uses a finer resolution for desaturated colours, to which we are more sensitive
- Colour difference is given as a ratio l:c, where
 - l scale factor for lightness
 - c scale factor for chroma
- To determine the perceptability of the difference between two colors, one sets l=c=1
 - Sometimes a ratio 2:1 is used
- To compute differences, one computes:

$$f = \sqrt{\frac{(\bar{C}^*)^4}{(\bar{C}^*)^4 + 1900}}$$

$$t = \begin{cases} 0.36 + 0.4 |\cos(35 + \bar{H})| & \text{if } \bar{H} \leq 164^\circ \vee \bar{H} > 345^\circ \\ 0.56 + 0.2 |\cos(168 + \bar{H})| & \text{if } 164^\circ < \bar{H} \leq 345^\circ. \end{cases}$$

- Following values define an ellipsoid in LCH colour space

$$S_L = \begin{cases} \frac{0.040975 L^*}{1 + 0.01765 \bar{L}^*} & \text{for } \bar{L}^* > 16, \\ 0.511 & \text{for } \bar{L}^* \leq 16, \end{cases}$$

$$S_C = \frac{0.0638 \bar{C}^*}{1 + 0.0131 \bar{C}^*} + 0.638,$$

$$S_H = S_C (ft + 1 - f).$$

where $\bar{L}^* = 0.5(L_1^* + L_2^*)$

and similarly C and H are averages.

- Finally def. the colour difference ΔE_{CMC} , which measures perceived difference:

$$\Delta L_{\text{CMC}} = \frac{L_1^* - L_2^*}{l S_L},$$

$$\Delta C_{\text{CMC}} = \frac{C_1^* - C_2^*}{c S_C},$$

$$\Delta H_{\text{CMC}} = \frac{H_1^* - H_2^*}{S_H},$$

$$\Delta E_{\text{CMC}} = \sqrt{\Delta L_{\text{CMC}}^2 + \Delta C_{\text{CMC}}^2 + \Delta H_{\text{CMC}}^2}$$

Colour Difference Metrics: CIE 1994

- CIE 1994 is improvement of CIE L*a*b* colour difference
- It specifies a set of experimental conditions under which the formula is valid
 - D65 illumination of color patches set side by side
 - Each patch covers at least 4°
 - Illuminance at 1000 lux.
- Also derives from CIE LCH, and is parametrized by weights k_L, k_C and k_H usually set to 1.

- Computes first

$$S_L = 1,$$

$$S_C = 1 + 0.045 \sqrt{C_1^* C_2^*}$$

$$S_H = 1 + 0.015 \sqrt{C_1^* C_2^*}$$

- Then $\Delta L_{94} = \frac{L_1^* - L_2^*}{k_L S_L},$

$$\Delta C_{94} = \frac{C_1^* - C_2^*}{k_C S_C},$$

$$\Delta H_{94} = \frac{H_1^* - H_2^*}{k_H S_H}.$$

from which the metric ΔE_{94}^*

$$\Delta E_{94}^* = \sqrt{\Delta L_{94}^2 + \Delta C_{94}^2 + \Delta H_{94}^2}.$$

- It works well, except for saturated blue and near neutral colors

Colour Difference Metrics: CIEDE2000

- Additional improvement for where CIE94 did not work well
- Derived from CIELAB
- Given two colors, one computes for each

$$C_{ab}^* = \sqrt{(a^*)^2 + (b^*)^2}$$

and the average of the two \bar{C}_{ab}^*

- Then

$$g = 0.5 \left(1 - \sqrt{\frac{(\bar{C}_{ab}^*)^7}{(\bar{C}_{ab}^*)^7 + 25^7}} \right)$$

- From this value, one computes for each color

$$L' = L^*,$$

$$a' = (1 + g)a^*,$$

$$b' = b^*,$$

$$C' = \sqrt{(a')^2 + (b')^2},$$

$$h' = \frac{180}{\pi} \tan^{-1} \left(\frac{b'}{a'} \right)$$

- One computes additional intermediate values:

$$R_C = 2 \sqrt{\frac{(\bar{C}')^7}{(\bar{C}')^7 + 25^7}},$$

$$R_T = -R_C \sin \left(60 \exp \left(- \left(\frac{\bar{h}' - 275}{25} \right)^2 \right) \right),$$

$$T = 1 - 0.17 \cos(\bar{h}' - 30) + 0.24 \cos(2\bar{h}') \\ + 0.32 \cos(3\bar{h}' + 6) - 0.20 \cos(4\bar{h}' - 63)$$

from which

$$S_L = 1 + \frac{0.015 (\bar{L}' - 50)^2}{\sqrt{20 + (\bar{L}' - 50)^2}}$$

$$S_C = 1 + 0.045 \bar{C}',$$

$$S_H = 1 + 0.015 \bar{C}' T.$$

Colour Difference Metrics: CIEDE2000

- Now we can finally compute the colour difference metric:

$$\Delta L_{\text{CIE00}} = \frac{L_1^* - L_2^*}{k_L S_L}$$

$$\Delta C_{\text{CIE00}} = \frac{C_1^* - C_2^*}{k_C S_C}$$

$$\Delta H_{\text{CIE00}} = \frac{2 \sin\left(\frac{h'_1 - h'_2}{2}\right) \sqrt{C'_1 C'_2}}{k_H S_H},$$

$$\Delta E_{\text{CIE00}} = \sqrt{\Delta L_{\text{CIE00}}^2 + \Delta C_{\text{CIE00}}^2 + \Delta H_{\text{CIE00}}^2 + R_T \Delta C_{\text{CIE00}} \Delta H_{\text{CIE00}}}$$

Colour Difference Metrics: comparison

original



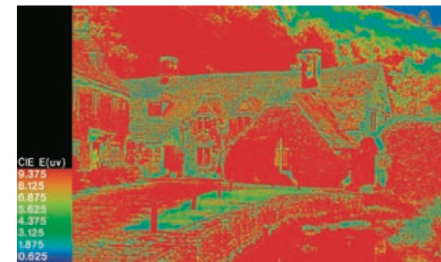
sharpened



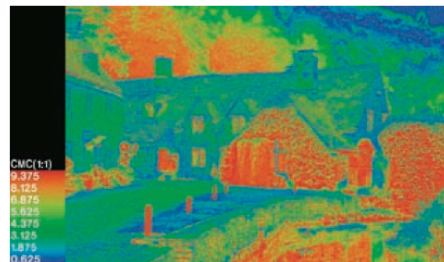
CIE e(ab)



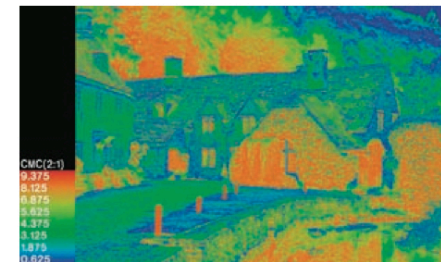
CIE E(uv)



CMC(1,1)



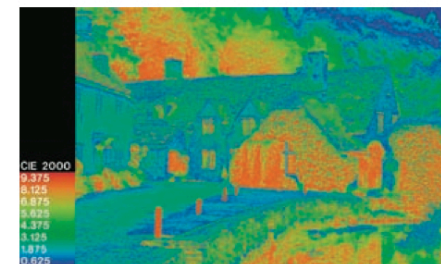
CMC(2,1)



CIE 94

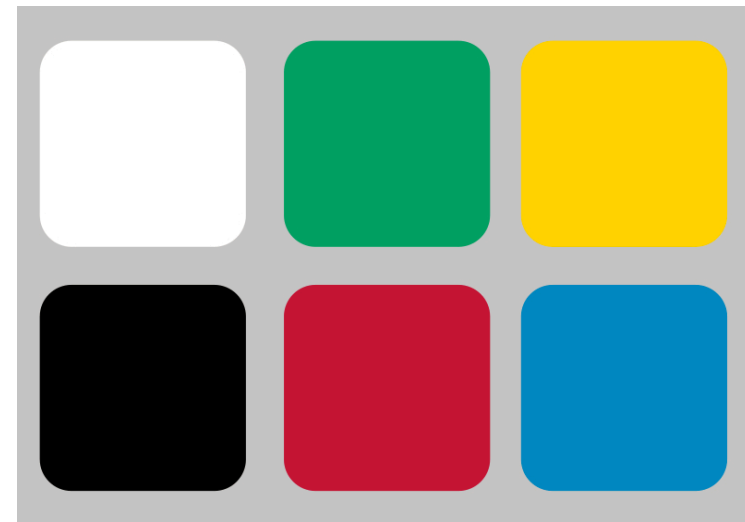
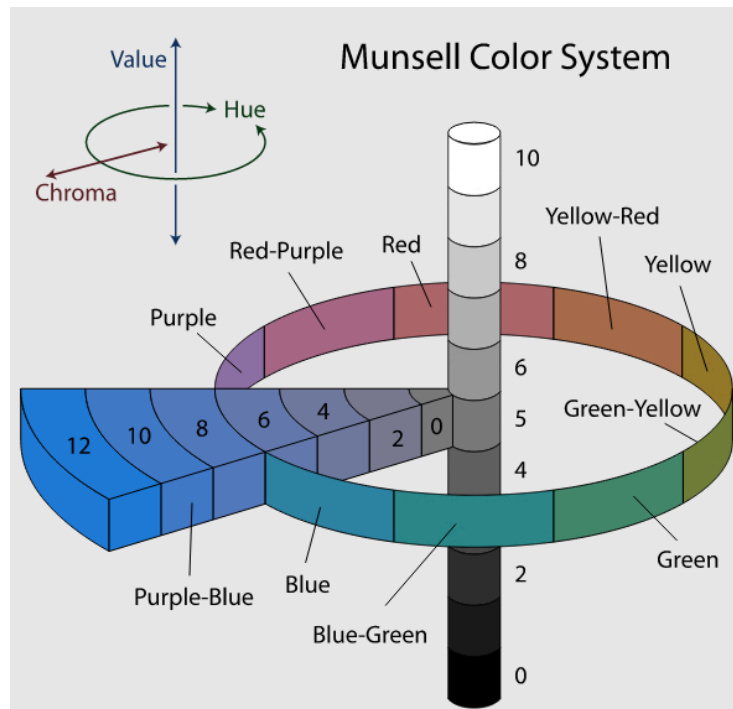


CIE 2000



Colour Order Systems

- These are a conceptual system of organized colour perception
- Munsell color system:
- Natural color system:
 - Blackness (darkness)
 - Chromaticity (saturation)
 - % of red, yellow, green, blue



- OSA colour system

Applications

- This knowledge can be used for:
 - Color matching and transfer between images
 - Principal component analysis to match colour spaces between images
 - Converting colour images to gray images
 - Rendering into complex colour spaces (not RGB)
 - Simulating painting methods
- In image understanding, classifying edges:
 - Shadow edges
 - Reflectance edges
- Understanding illuminance features

Thank you!

- Thank you for your attention!
- Web pages
<http://www.uni-weimar.de/medien/cg>